

APPENDIX A

% BEGINNING OF PSEUDO CODE

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5      % compute scale factor A, and time constants a, b from physical system
      % parameters

    A = Vmax * Kt / (Re * Rm + Kt * Kb) * l * k;

10     p1 = 1/Jm/Ie * (-Ie * Rm - Re * Jm + sqrt(Ie^2 * Rm^2 - 2 * Re * Rm * Ie * Jm
      + Re^2 * Jm^2 - 4 * Kt * Kb * Ie * Jm)) / 2;
      p2 = 1/Jm/Ie * (-Ie * Rm - Re * Jm - sqrt(Ie^2 * Rm^2 - 2 * Re * Rm * Ie * Jm
      + Re^2 * Jm^2 - 4 * Kt * Kb * Ie * Jm)) / 2;

15     a = max(-p1,-p2)
      b = min(-p1,-p2)

      % make initial guesses for step durations

20     et1 = 1;
      et2 = .005;
      et3 = 1;

      % set maximum iteration count

25     Nmax = 1000;

      for j = 1:Nmax
          % save old values of step time intervals
30     et3old = et3;
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et2old = et2;
et1old = et1;

% iterate for switch times using fixed voltage level Vmax

5
et3 = -log(1.0 / 2.0 - exp(-et1 * a) / 2 + exp(-et2 * a)) / a;
et2 = 1/b * log(2.0) + 3 * et3 - 1/b * log(2 * exp(1/A * b * X) * exp(et3
* b) - sqrt( 4.0) * sqrt(exp(1/A * b * X)) * exp(et3 * b) *
sqrt(exp(1/A * b * X)+exp(et3 * b)^2 - 2 * exp(et3 * b)));
et1 = - (-2 * A * et2 + 2 * A * et3 - X) / A;

10

if norm([et3old - et3 et2old - et2 et1old - et1], inf) <= eps * 2
    break
end

15
if j==Nmax
    error(['error - failure to converge after ', num2str(Nmax),'
iterations'])
end
end

20

% round up pulse duration to nearest sample interval,
% convert to intervals between steps to make sure that voltage
% requirements will not increase (beyond Vmax).

dt1=ceil((et1 - et2) / dt) * dt;
dt2=ceil((et2 - et3) / dt) * dt;
dt3=ceil((et3) / dt) * dt;

et123 = [et1, et2, et3]

30
% convert back to total step duration.

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et1 = dt1 + dt2 + dt3;

et2 = dt2 + dt3;

et3 = dt3;

5 % In the following, the original constraints equations involving XF1, XF2,
% and XF3 have been modified to include a variable voltage level applied
at

% each step (instead of the fixed maximum (+/-) Vmax).

10 % The original equations for XF1, XF2, and XF3 follow:

% XF1(t_{end}) = V₀F₁(t_{end} - t₀) - 2V₀F₁(t_{end} - t₁) + 2V₀F₁(t_{end} - t₂)

% XF2(t_{end}) = V₀F₂(t_{end} - t₀) - 2V₀F₂(t_{end} - t₁) + 2V₀F₁(t_{end} - t₂)

% XF3(t_{end}) = V₀F₃(t_{end} - t₀) - 2V₀F₂(t_{end} - t₁) + 2V₀F₁(t_{end} - t₂)

15 % And the modified equation including adjustable relative levels of
voltage

% L1, L2 and L3 are:

% XF1(t_{end}) = L₁V₀F₁(t_{end} - t₀) - L₂V₀F₁(t_{end} - t₁) + L₃V₀F₁(t_{end} - t₂)

% XF2(t_{end}) = L₁V₀F₂(t_{end} - t₀) - L₂V₀F₂(t_{end} - t₁) + L₃V₀F₁(t_{end} - t₂)

20 % XF3(t_{end}) = L₁V₀F₃(t_{end} - t₀) - L₂V₀F₂(t_{end} - t₁) + L₃V₀F₁(t_{end} - t₂)

% And the corresponding constraint equations are:

% XF1(t_{end}) = Finalpos

% XF2(t_{end}) = 0

25 % XF3(t_{end}) = 0

% Where all of the times indicated have discrete values, e.g.
corresponding to

% the controller update rate.

30

% It should be noted that after the digital switch times are fixed, the constraint

% equations derived from the equations above form a linear set of equations in

5 % the unknown relative voltage levels L1, L2 and L3 and any standard linear

% method can be used to solve for the relative voltage levels. In the equations

10 % for (L1, L2 and L3) that follow, the solution was obtained by algebraic
% means (and are not particularly compact.)

% compute new relative voltage step levels

% L1, L2 and L3 are nominally assigned to "1", "-2" and "+2", respectively

15 s1 = X * (exp(-et3 * b) * exp(-et2 * a) + exp(-et3 * a) + exp(-et2 * b) - exp(-et2 * b) * exp(-et3 * a) - exp(-et2 * a) - exp(-et3 * b));

s2 = 1 / (et2 * exp(-et1 * b) * exp(-et3 * a) + exp(-et2 * b) * et3 *
exp(-et1 * a) - et2 * exp(-et3 * a) - et2 * exp(-et1 * b) - et3 *
exp(-et1 * a) - exp(-et2 * b) * et3 + exp(-et3 * b) * et1 * exp(-et2 *
20 a) + exp(-et3 * a) * et1 + exp(-et2 * b) * et1 - exp(-et2 * b) * et1 *
exp(-et3 * a) - et3 * exp(-et1 * b) * exp(-et2 * a) - exp(-et2 * a) *
et1 - exp(-et3 * b) * et1 - exp(-et3 * b) * et2 * exp(-et1 * a) + et3 *
exp(-et1 * b) + et2 * exp(-et1 * a) + exp(-et3 * b) * et2 + et3 *
exp(-et2 * a)) / A;

25

L1 = s1 * s2;

s1 = 1 / (et2 * exp(-et1 * b) * exp(-et3 * a) + exp(-et2 * b) * et3 *
exp(-et1 * a) - et2 * exp(-et3 * a) - et2 * exp(-et1 * b) - et3 *
30 exp(-et1 * a) - exp(-et2 * b) * et3 + exp(-et3 * b) * et1 *

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exp(-et2 * a) + exp(-et3 * a) * et1+exp(-et2 * b) * et1 -
exp(-et2 * b) * et1 * exp(-et3 * a) - et3 * exp(-et1 * b) *
exp(-et2 * a) - exp(-et2 * a) * et1 - exp(-et3 * b) * et1 - exp(-et3 *
b) * et2 * exp(-et1 * a) + et3 * exp(-et1 * b) + et2 * exp(-et1 * a) +
5      exp(-et3 *b ) * et2 + et3 * exp(-et2 * a)) * X;

s2 = (exp(-et2 * b) * exp(-et1 * a) - exp(-et1 * a) - exp(-et2 * b) -
exp(-et1 * b) * exp(-et2 * a) + exp(-et1 * b) + exp(-et2 * a)) / A;
L3 = s1*s2;

10    s1 = exp(-et1 * a) - exp(-et3 * a) + exp(-et3 * b) - exp(-et1 * b) -
exp(-et3 * b) * exp(-et1 * a) + exp(-et1 * b) * exp(-et3 * a);
s2 = X / (et2 * exp(-et1 * b) * exp(-et3 * a) + exp(-et2 * b) * et3 *
exp(-et1 * a) - et2 * exp(-et3 * a) - et2 * exp(-et1 * b) - et3 *
exp(-et1 * a) - exp(-et2 * b) * et3 + exp(-et3 * b) * et1 * exp(-et2 *
15      a) + exp(-et3 * a) * et1 + exp(-et2 * b) * et1 - exp(-et2 * b) * et1 * exp(-
et3 * a) - et3 * exp(-et1 * b) * exp(-et2 *a ) - exp(-et2 * a) * et1-exp(-et3 *
b) * et1 - exp(-et3 * b) * et2 * exp(-et1 * a) + et3 *
exp(-et1 * b) + et2 * exp(-et1 * a) + exp(-et3 * b) * et2 + et3 *
exp(-et2 * a)) / A;
20
L2 = s1 * s2;

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% convert accumulated voltage steps to sequential voltage level
V1 = Vmax * (L1);
25
V2 = Vmax * (L1 + L2);
V3 = Vmax * (L1 + L2 + L3);

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% END OF PSEUDO CODE
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APPENDIX B

```
AREA .. SUM(I,A(I)) =E= 0;  
VELOCITY(VINDX) .. VEL(VINDX) =E= VSCALE *  
5 SUM(I$(ORD(I) LE ORD(VINDX)), A(I));  
POSITION .. SUM(I,VEL(I)) =E= FINALPOS * SCALEFACT;  
VLIMITP(I) .. SUM(VINDX$(ORD(VINDX) LE ORD(I)),A(I-  
(ORD(VINDX)+1))*(VOLTS(VINDX)+KBACK*VSCALE))  
=L= VOLTLIM;  
10 VLIMITN(I) .. SUM(VINDX$(ORD(VINDX) LE ORD(I)), A(I-  
(ORD(VINDX)+1))*(VOLTS(VINDX)+KBACK*VSCALE))  
=G= -VOLTLIM  
  
% A(I) are the current commands at time T(I) spaced equally at time DT.  
15 % VOLTS(VINDX) is a table of voltages representing the unit pulse  
response to  
% a unit output in current command. VOLTLIM is the voltage limit at  
saturation.
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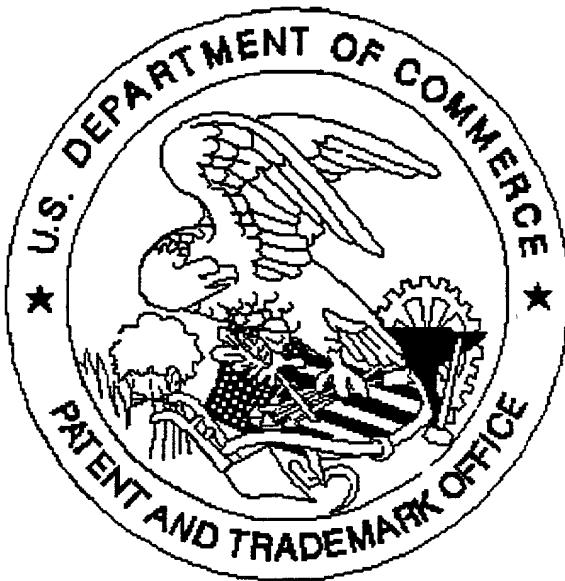
APPENDIX C

GOALPOS .. SUM(I,A(I)*MODELAA*DT) =E=FINALPOS;
MODE1(ILAST) .. SUM(I,-A(I)*MODELAA*MODELb/(MODELb-
5 MODELa)*(EXP(-MODELa*(T(ILAST)+DT-T(I)))-
-EXP(-MODELa*(T(ILAST)-T(I)))) =E= 0.0;
MODE2(ILAST) .. SUM(I,A(I)*MODELAA*MODELa/(MODELb-
MODELa)*(EXP(-MODELb*(T(ILAST)+DT-T(I)))-
-EXP(-MODELb*(T(ILAST)-T(I)))) =E= 0.0;
10 DERIV1(J) .. 1000.0*SUM(I,A(I)*T(I)*EXP(ZETA(J)*W(J)*T(I))*
SIN(WD(J)*T(I))) =E= 0.0 ;
DERIV2(J) .. 1000.0*SUM(I,A(I)*T(I)*EXP(ZETA(J)*W(J)*T(I))*
COS(WD(J)*T(I))) =E= 0.0 ;

15 % MODELAA is the mechanical gain of the system, MODELb, and MODELa
% are the two time constants of the system in radians. One time constant is
% associated with the L/R rise time of the motor inductance and the other is
% the mechanical time constant of the rigid system. The A(I) are the voltages %
which need to be determined. The T(I) are the times for each of the A(I).
20 % DT is the time spacing of the outputs. W(J) are the undamped flexible
% modes, WD(J) are the damped flexible modes (in radians/s).

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